

ECE 463/663 - Homework #5

Full State Feedback. Due Monday, February 24th

1) Write a Matlab m-file which is passed

- The system dynamics (A, B),
- The desired pole locations (P)

and then returns the feedback gains, K_x , so that $\text{roots}(A - B K_x) = P$

Problems 2-4) Assume the following dynamic system:

$$sX = \begin{bmatrix} -10 & 5 & 0 & 0 & 0 \\ 5 & -10 & 5 & 0 & 0 \\ 0 & 5 & -10 & 5 & 0 \\ 0 & 0 & 5 & -10 & 5 \\ 0 & 0 & 0 & 5 & -5 \end{bmatrix} X + \begin{bmatrix} 5 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix} U$$
$$Y = \begin{bmatrix} 0 & 0 & 0 & 0 & 1 \end{bmatrix} X$$

2) (20 points) Find the feedback control law of the form

$$U = K_r R - K_x X$$

so that

- The DC gain is 1.000 and
- The closed-loop poles are at $\{-1, -2, -3, -4, -5\}$

Plot

- The resulting closed-loop step response, and
- The resulting input, U

3) (20 points) Repeat problem #2 but find K_x and K_r so that

- The DC gain is 1.000 and
- The closed-loop dominant pole is at $s = -1$ and the other four poles don't move (they are the same as the fast four poles of the open-loop system (eigenvalues of A))

Plot

- The resulting closed-loop step response, and
- The resulting input, U

4) (over)

4) (20 points) Repeat problem #2 but find K_x and K_r so that

- The DC gain is 1.000
- The 2% settling time is 2 seconds, and
- There is 10% overshoot for a step input.

Plot

- The resulting closed-loop step response, and
- The resulting input, U