

ECE 463/663 - Homework #4

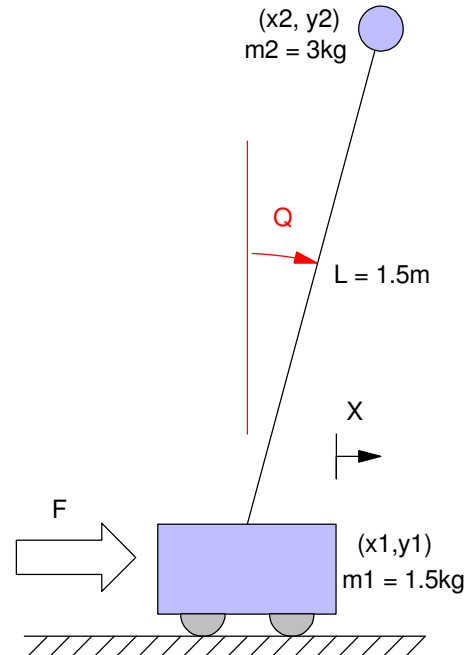
LaGrangian Dynamics. Due Monday, February 10th

Cart & Pendulum

1) (30pt) Derive the dynamics for an inverted pendulum where

- $m_1 = 1.5\text{kg}$ (mass of cart)
- $m_2 = 3\text{kg}$ (mass of ball)
- $L = 1.5\text{m}$ (length of arm)

Find the linearized dynamics at $x = 0, \theta = 0$



Ball and Beam

2) (30pt) Derive the dynamics for a ball and beam system where

- $J = 0.7\text{ kg m}^2$ (the inertia of the beam)
- $m = 2.2\text{ kg}$ (the mass of the ball)

Find the linearized dynamics at $r = 1.0\text{m}, \theta = 0$

