

# ECE 341 - Homework #12

t-Test with a Single Population. Summer 2024

## 6-Card Stud Poker

The computed odds of being dealt a full-house in 6-card poker are in homework set #2.

1) The result of four Monte-Carlo simulations with 100,000 poker hands are:

811 805 809 804

From these results, determine the 90% confidence interval for the odds of being dealt a full-house

The t-score for 5% tails and 3 degrees of freedom (sample size = 4) is

$$t = 2.355$$

**The 90% confidence interval is (803.3595, 811.1405)**

- calculated odds: 815.3048 in 100,000 hands
- The data suggests the calculations were slightly high

Note: This is a population question (trying to find the population's mean). Divide the variance by the sample size

```
>> Data = [811 805 809 804 ];
>> x = mean(Data)

x = 807.2500

>> s = std(Data) / sqrt(4)

s = 1.6520

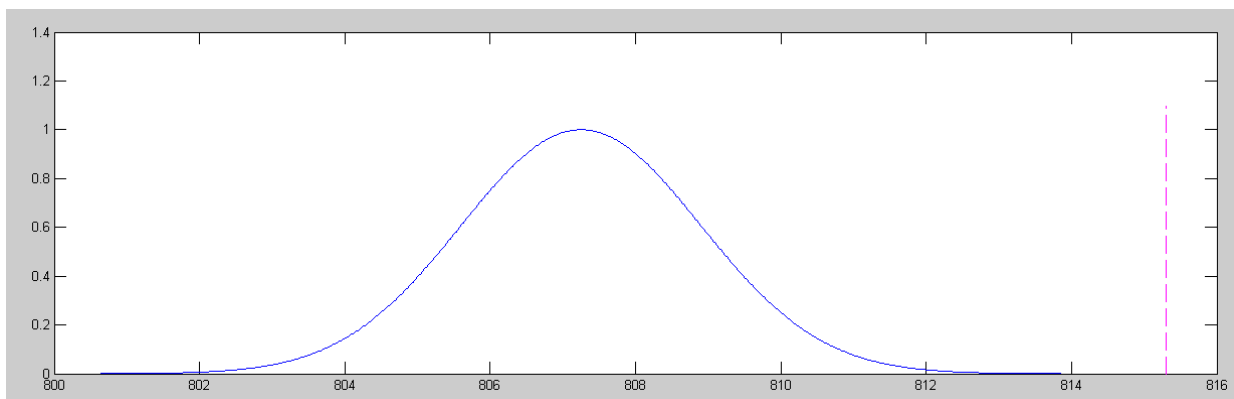
>> x + 2.355*s

ans = 811.1405

>> x - 2.355*s

ans = 803.3595

>>
```



## 6-Card Stud Poker

2) The result of twenty Monte-Carlo simulations with 100,000 poker hands are:

```
811 805 809 804 837 830 841 770 889 821
850 754 786 763 754 855 785 724 815 823
```

From these results, determine the 90% confidence interval for the odds of getting a full-house.

- The t-score for 5% tails and 19 degrees of freedom is 1.729

**The 90% confidence interval is (790.7496, 821.8504) in 100,000 hands**

- Calculated odds are 815.3048 in 100,000 hands
- This *is* within the calculated 90% confidence interval, so calculations *might* be correct

```
>> DATA = [811 805 809 804 837 830 841 770 889 821 850 754
786 763 754 855 785 724 815 823];
>> x = mean(DATA)

x = 806.3000

>> n = length(DATA)

n = 20

>> s = std(DATA) / sqrt(n)

s = 8.9939

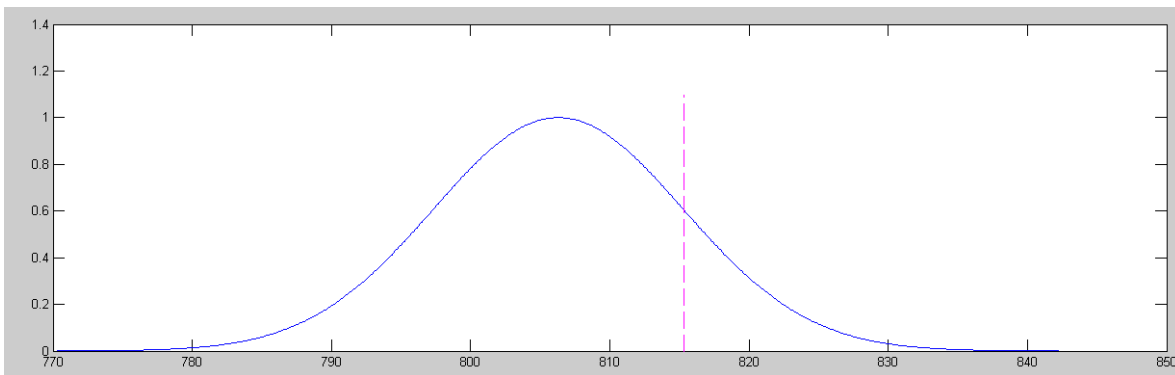
>> x + 1.729*s

ans = 821.8504

>> x - 1.729*s

ans = 790.7496

>>
```



## 6-Card Draw

The computed odds of getting a full house in 6-card poker with a draw step was found in homework #2

3) The result of four Monte-Carlo simulations with 100,000 poker hands are:

```
3747  3633  3764  3692
```

From these results, determine the 90% confidence interval for the odds of getting a full-house.

**90% confidence interval = (3639.2, 3778.8)**

- Calculated odds are 3570 in 100,000 hands

```
>> DATA = [3747  3633  3764  3692];  
>> n = length(DATA)
```

```
n =      4
```

```
>> x = mean(DATA)
```

```
x =      3709
```

```
>> s = std(DATA) / sqrt(n)
```

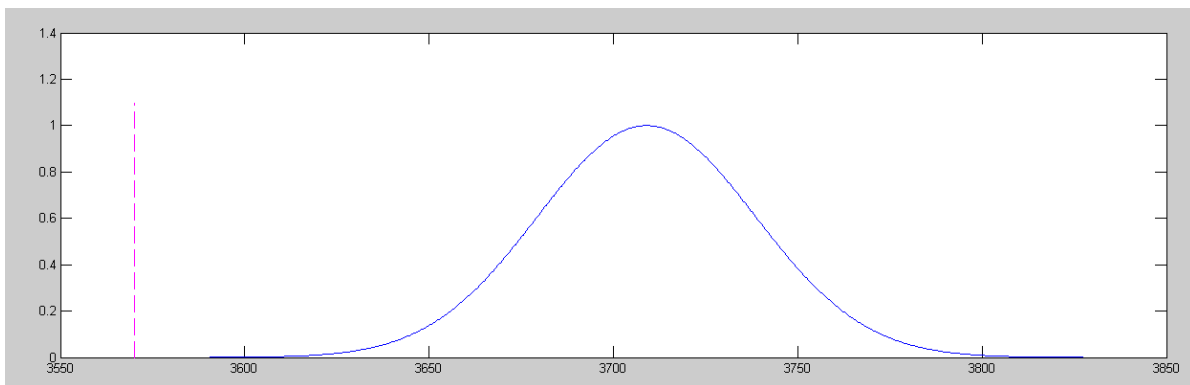
```
s =  29.6283
```

```
>> x + 2.355*s
```

```
ans =  3.7788e+003
```

```
>> x - 2.355*s
```

```
ans =  3.6392e+003
```



## 6-Card Draw (sample size = 20)

4) The result of twenty Monte-Carlo simulations with 100,000 poker hands are:

```
3747 3633 3764 3692 3760 3793 3778 3708 3786 3650
3664 3777 3744 3788 3739 3620 3701 3759 3848 3693
```

From these results, determine the 90% confidence interval for the odds of getting a full house.

**90% confidence interval = (3709.0, 3755.4)**

- Calculated odds are 3570 in 100,000 hands
- probably, the calculations are off or the Monte-Carlo simulation has errors

```
>> DATA = [3747 3633 3764 3692 3760 3793 3778 3708 3786 3650 3664 3777
3744 3788 3739 3620 3701 3759 3848 3693];

>> n = length(DATA)

n = 20

>> x = mean(DATA)

x = 3.7322e+003

>> s = std(DATA) / sqrt(n)

s = 13.4434

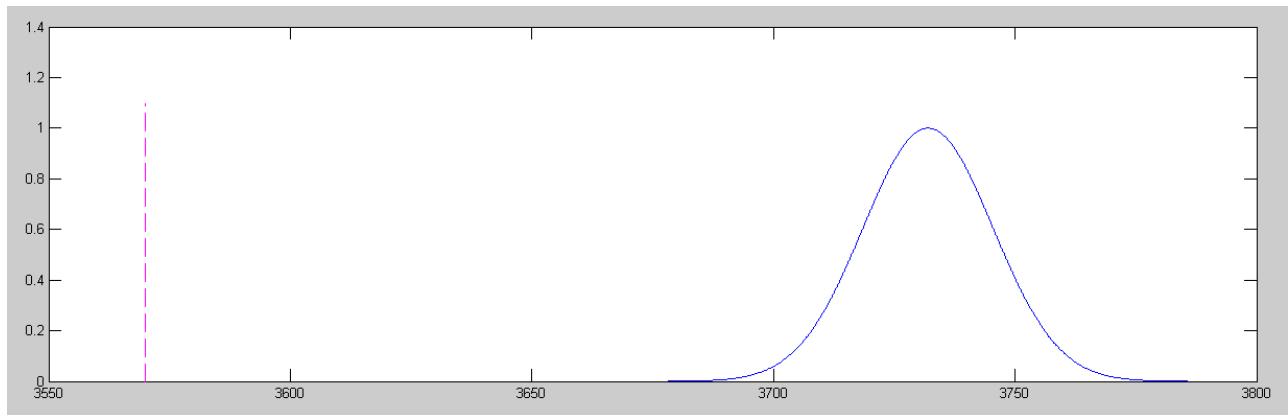
>> x + 1.729*s

ans = 3.7554e+003

>> x - 1.729*s

ans = 3.7090e+003

>>
```



Repeating with corrected code:

```
5663, 5833, 5576, 5602, 5587, 5623, 5787, 5751, 5579, 5730
```

```
>> DATA = [5663, 5833, 5576, 5602, 5587, 5623, 5787, 5751, 5579, 5730];  
>> x = mean(DATA)
```

```
x = 5.6731e+003
```

```
>> s = std(DATA)
```

```
s = 94.9918
```

```
>> s = std(DATA) / sqrt(10)
```

```
s = 30.0390
```

```
>> x + 1.833*s
```

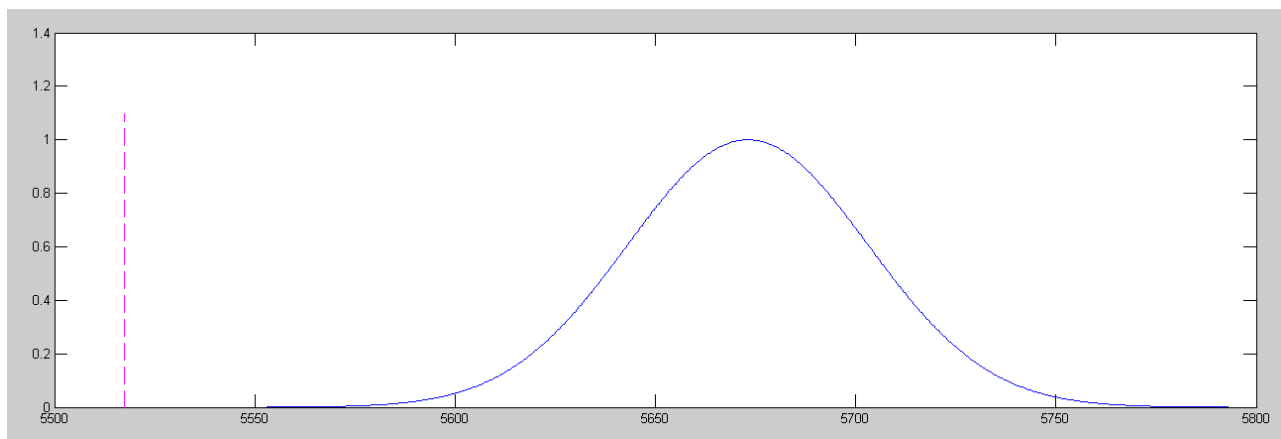
```
ans = 5.7282e+003
```

```
>> x - 1.833*s
```

```
ans = 5.6180e+003
```

**The 90% confidence interval is (5618.0, 5728.2)**

- Calculated odds are 5517.4
- It appears calculations were a little low



## Reaction Time

5) Go to the Human Benchmark Dashboard and record your reaction time

<https://humanbenchmark.com/tests/reactiontime>

Times: {230ms, 248ms, 233ms, 241ms}

6) From your results, determine the 90% confidence interval for your reaction time.

In this case, it's an individual test (one more trial) so you do not divide by the square-root of sample size

The 90% confidence interval for any given trial is (218.86ms, 257.13ms)

```
>> DATA = [230, 248, 233, 241];
>> x = mean(DATA)

x =    238

>> s = std(DATA)

s =    8.1240

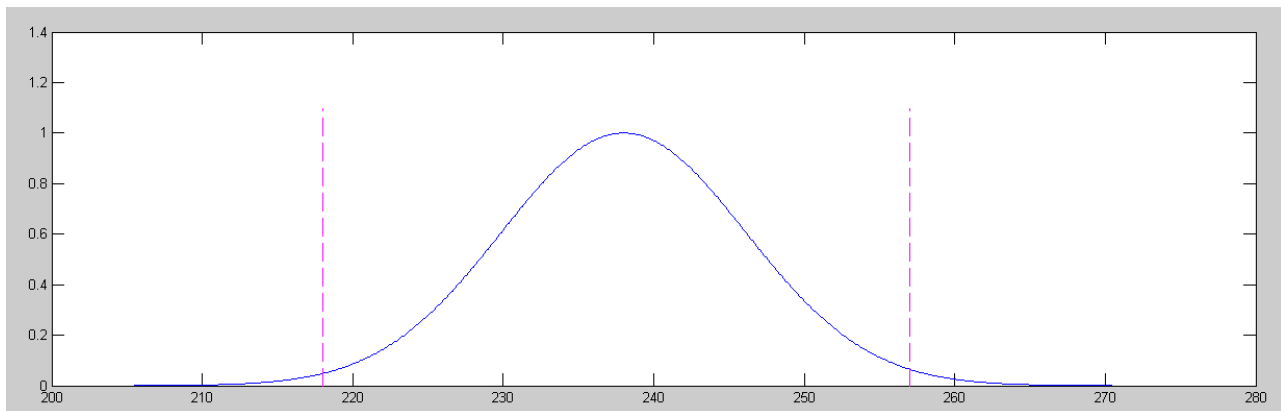
>> x + 2.355*s

ans =    257.1321

>> x - 2.355*s

ans =    218.8679

>>
```



7) From your results, determine the probability that

Your next trial will be less than 200ms

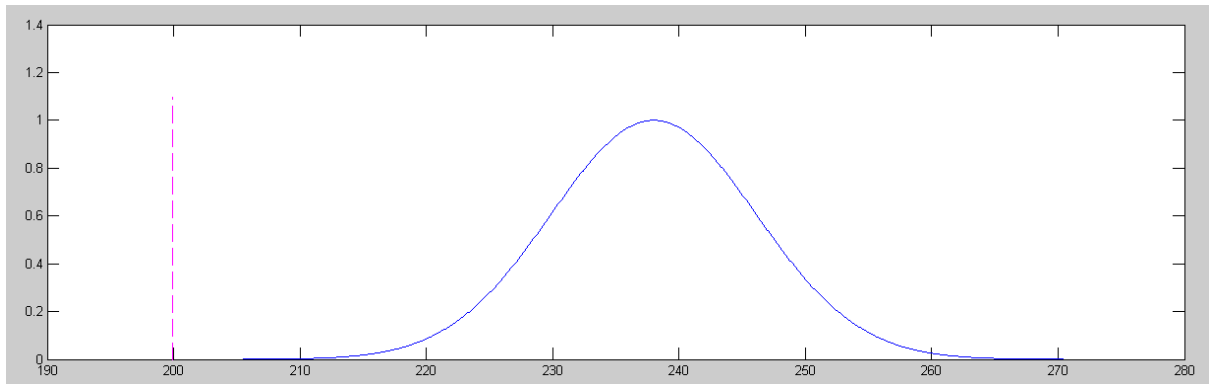
Individual Case. The t-score is

$$t = (200 - \bar{x}) / s$$

$$t = -4.6775$$

From StatTrek, a t-score of 4.6775 with 3 degrees of freedom corresponds to a probability of 0.009

**There is a 0.9% chance my next score will be less than 200ms**

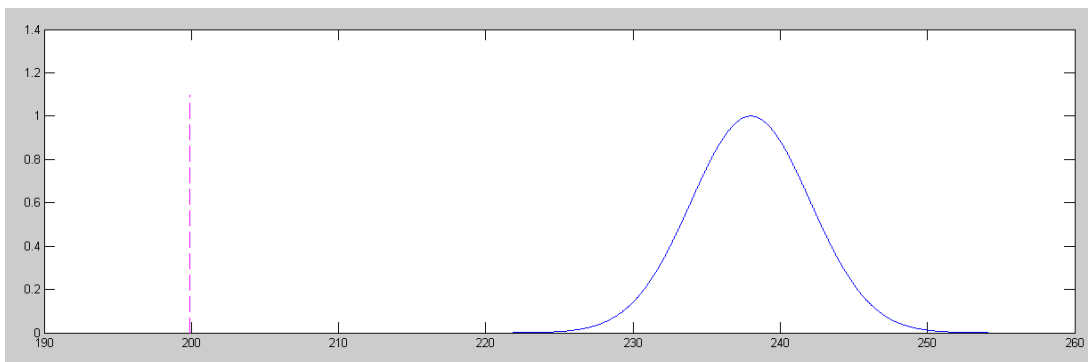


Your average reaction time is less than 200ms

Population (my average reaction time)

```
>> n = length(DATA)
n =      4
>> s = std(DATA) / sqrt(n)
s =      4.0620
>> t = (200 - x) / s
t =     -9.3550
```

From StatTrek this corresponds to a probability of 0.001



**There is a 0.1% chance my average score will is less than 200ms**

- In the dropdown box, select the statistic of interest.
- Enter a value for degrees of freedom.
- Enter a value for all but one of the remaining textboxes.
- Click the **Calculate** button to compute a value for the blank textbox.

Statistic	t score
Degrees of freedom	3
Sample mean ( $\bar{x}$ )	-9.3550
Probability: $P(X \leq -9.355)$	0.001

**Calculate**