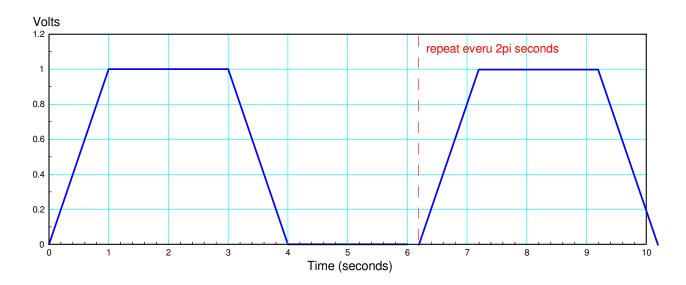
# **ECE 111 - Homework #15**

Week #15 - Signals & Frequency Content of a Signal

Problem 1-5) Let x(t) be a function which is periodic in  $2\pi$  as shown below

$$x(t) = x(t + 2\pi)$$

or in Matlab:



x(t) Note that x(t) repeats repeats every  $2\pi$  seconds

#### Curve Fitting with a power series:

1) Using least squares, approximate x(t) over the interval  $(0, 2\pi)$  as

$$x(t) \approx a_0 + a_1 t + a_2 t^2 + a_3 t^3 + a_4 t^4 + a_5 t^5$$

Plot x(t) along with it's approximation.

# **Curve Fitting using a Fourier Series**

2) Using least squares, approximate x(t) over the interval  $(0, 2\pi)$  as

$$x(t) = a_0 + a_1\cos(t) + b_1\sin(t) + a_2\cos(2t) + b_2\sin(2t) + a_3\cos(3t) + b_3\sin(3t)$$

Plot x(t) along with it's approximation.

### **Curve Fitting using a Fourier Series (take 2)**

3a) Determine x(t) in terms of its Fourier Transform out to 3 rad/sec

$$a_0 = mean(x)$$

$$a_n = 2 \cdot mean(x \cdot \cos(nt))$$

$$b_n = 2 \cdot mean(x \cdot \sin(nt))$$

3b) Plot x(t) and its Fourier approximation taken out to 3 rad/sec

## **Superposition**

Assume X and Y are related by

$$Y = \left(\frac{1}{s^2 + s + 1}\right) X$$

- 4) Determine the output, y(t), at DC (w = 0)
- 5) Determine the output, y(t), at 1 rad/sec
- 6) Determine the output, y(t), at 2 rad/sec
- 7) Determine the output, y(t), at 3 rad/sec
- 8) Determine the total answer, y(t)
  - Plot x(t) and y(t)