

ECE 343 - Homework #1

Complex Numbers and Phasors - Summer 2018

Complex Numbers

Solve for Y

$$1) \quad Y = \left(\frac{10(s+3)}{s(s+2)(s+10)} \right)_{s=j5}$$

$$2) \quad Y = \left(\frac{20}{s^3+4s^2+6s+10} \right)_{s=-1+j3}$$

$$3) \quad Y = e^{-2+j3}$$

$$4) \quad Y = (1+j2) + \left(\frac{1}{3+j4} + \frac{1}{5+j6} \right)^{-1}$$

$$5) \quad \begin{bmatrix} 1 & 1+j & 0 \\ 1+j & 2 & j5 \\ 0 & j5 & 3-j \end{bmatrix} Y = \begin{bmatrix} 1 \\ j2 \\ 1-j2 \end{bmatrix}$$

Phasors

Determine the phasor representation for y(t)

$$6) \quad y(t) = 3 \cos(5t) + 6 \sin(5t)$$

$$7) \quad y(t) = -3 \cos(6t - 20^\circ) + 7 \sin(6t + 50^\circ)$$

Determine y(t) using phasor analysis

$$8) \quad \frac{d^2y}{dt^2} + 3\frac{dy}{dt} + 20y = 5\frac{dx}{dt} + 10x$$

$$x(t) = 3 \cos(4t)$$

$$9) \quad \frac{d^3y}{dt^3} + 6\frac{d^2y}{dt^2} + 11\frac{dy}{dt} + 24y = 48x$$

$$x(t) = 4 \cos(3t) + 2 \sin(3t)$$