

# ECE 321 - Quiz #3 - Name \_\_\_\_\_

BJT Amplifiers & 2-Port Models

1) BJT Amplifier: DC Analysis. Determine the Thevenin equivalent of R<sub>1</sub> and R<sub>2</sub> as well as the Q-point. Assume ideal silicon transistors:

- |V<sub>be</sub>| = 0.7V
- $\beta = 40$
- $R_2 = 1100 + 100 \cdot (\text{your birth month}) + (\text{your birth day})$ . May 14th would give  $R = 1614$  Ohms

$R_2$ 1100 + 100*mo + day	V <sub>b</sub>	R <sub>b</sub>	V <sub>ce</sub>	I <sub>c</sub>
<b>1614</b>	<b>1.668V</b>	<b>1390</b>	<b>9.17V</b>	<b>311uA</b>

$$R_b = R_1 \parallel R_2 = 1390\Omega$$

$$V_b = \left( \frac{R_2}{R_1 + R_2} \right) 12V = 1.668V$$

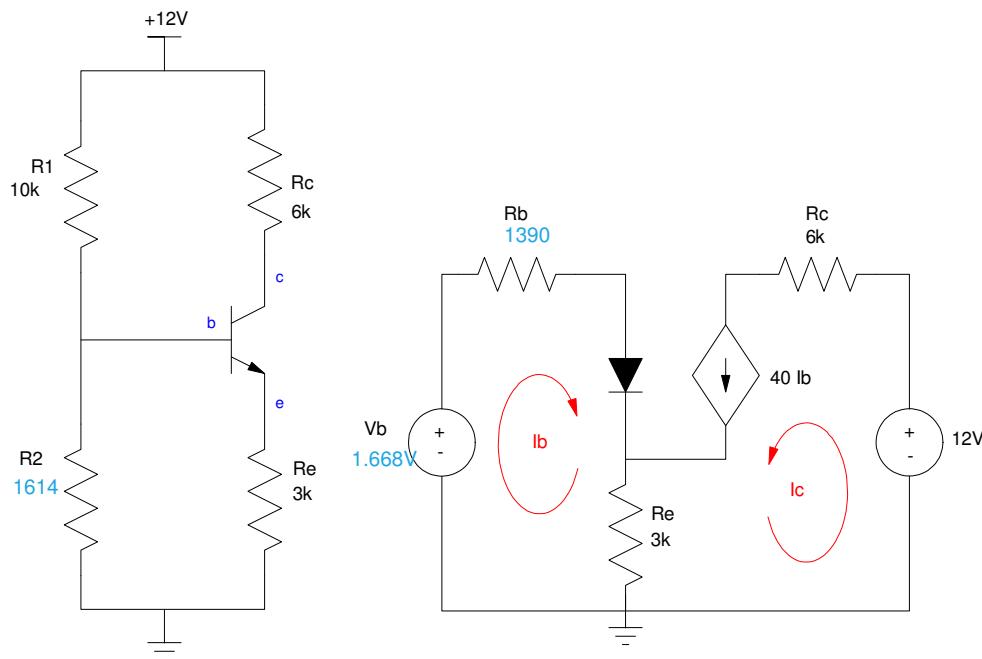
$$I_b = \left( \frac{1.668V - 0.7V}{1390 + 41 \cdot 3k} \right) = 7.77\mu A$$

$$I_c = 40I_b = 311.1\mu A$$

$$V_c = 12 - 6k \cdot I_c = 10.133V$$

$$V_e = 3k \cdot (I_b + I_c) = 0.9568V$$

$$V_{ce} = V_c - V_e = 9.17V$$



2) BJT Amplifier: DC Design. Determine R1 and R2 so that

- The Q point is Vce = 6.00V and
- The Q point is stabilized for variations in  $\beta$

Assume

- Ideal silicon transistors ( $V_{be} = 0.7V$ ,  $\beta = 40$ )
- $R_c = 1100 + 100 \cdot (\text{birth month}) + (\text{birth day})$ . May 14th gives  $R_c = 1614$  Ohms

$R_c$ $1100 + 100 \cdot \text{mo} + \text{day}$	R1	R2	Vb	Rb
<b>1614</b>	<b>22.43k</b>	<b>4.86k</b>	<b>2.1395V</b>	<b>4k</b> $\ll 41k$

$$6V = R_c I_c + R_e (I_b + I_c)$$

$$I_c = \left( \frac{6V}{1614 + 3000 \left(1 + \frac{1}{40}\right)} \right) = 1.280mA$$

$$I_b = \frac{I_c}{40} = 31.99\mu A$$

To stabilize the Q-point

$$R_b \ll (1 + \beta) R_e = 41k\Omega$$

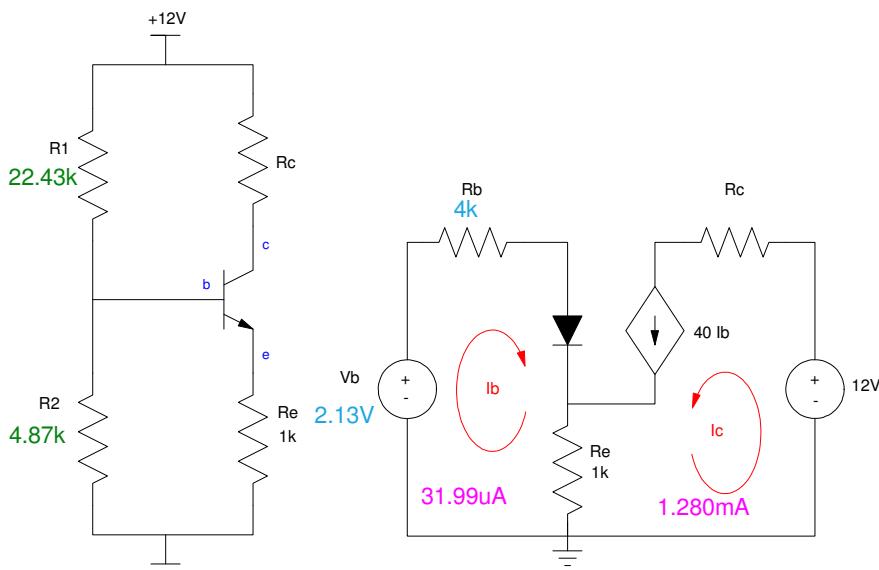
Let  $R_b = 4k$

$$V_b = I_b R_b + 0.7 + R_e (I_e + I_c) = 2.1395V$$

Solve for R1 and R2

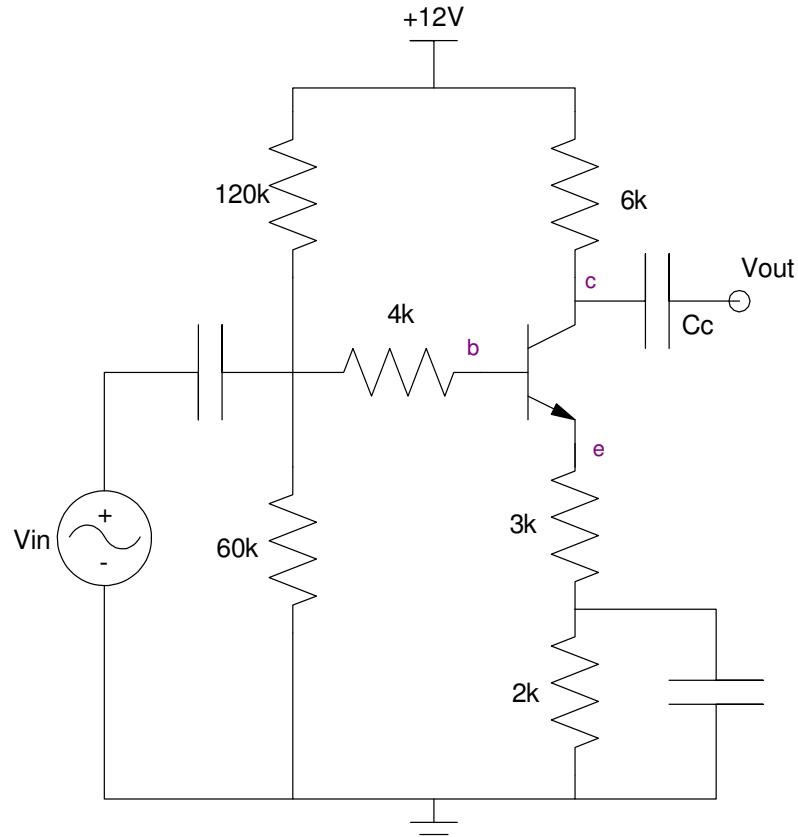
$$R_1 = \left( \frac{12V}{2.1395V} \right) 4k = 22.43k\Omega$$

$$R_2 = 4.8679k\Omega$$

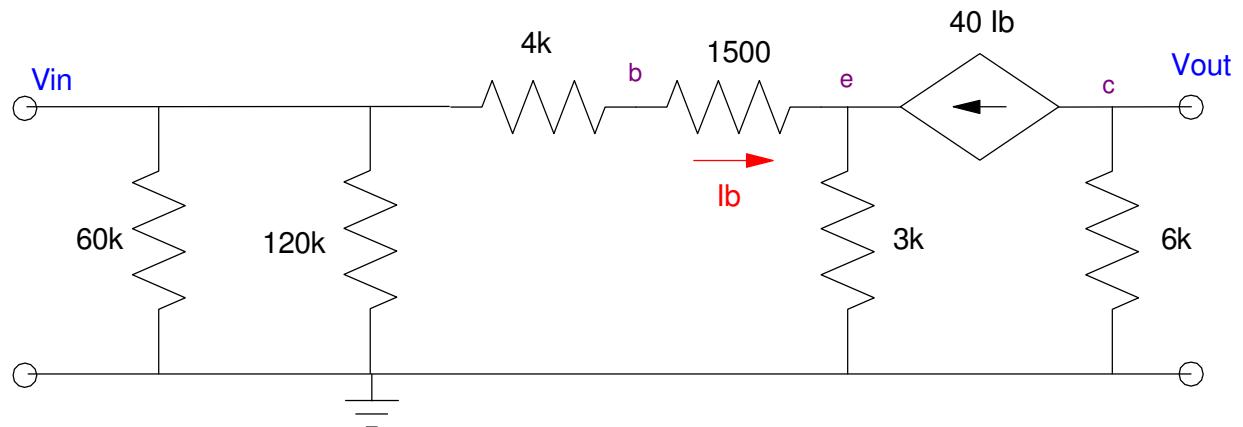


3) BJT: AC Analysis: Draw the small signal model for the following BJT amplifier. Assume

- $r_f = 1500\Omega$
- $\beta = 40$

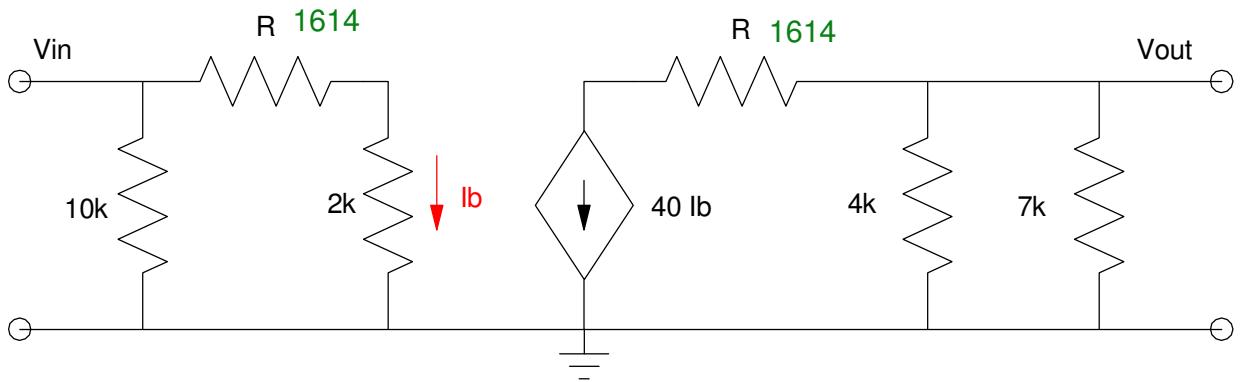


answer:



4) 2-Port Models. Determine the 2-port model for the following circuit:

R 1100 + 100*mo + day	Rin	Ain	Rout	Ao
<b>1614</b>	<b>2655</b> varies with R	<b>0</b>	<b>2524</b>	<b>-28.17</b> varies with R



$$R_{in} = 10k \parallel (1614 + 2000) = 2655\Omega$$

$$A_{in} = 0$$

$$R_{out} = 4k \parallel 7k = 2524\Omega$$

$$A_o = -\left(\frac{1}{1614+2000}\right)(40)(4k \parallel 7k) = -28.17$$

5) 2-Port model (experimental): Determine the 2-port parameters based upon the following experimental data:

Case 1:

- $V_{in} = 1\text{mV}$  @ 1kHz
- $R_1 = 0 \text{ Ohms}$
- $R_2 = 10\text{M Ohms}$

results in  $V_{out} = 57\text{mV}$

Case 2:

- $V_{in} = 1\text{mV}$  @ 1kHz
- $R_1 = X \text{ Ohms}$
- $R_2 = 10\text{M Ohms}$

results in  $V_{out} = 43\text{mV}$

Case 3

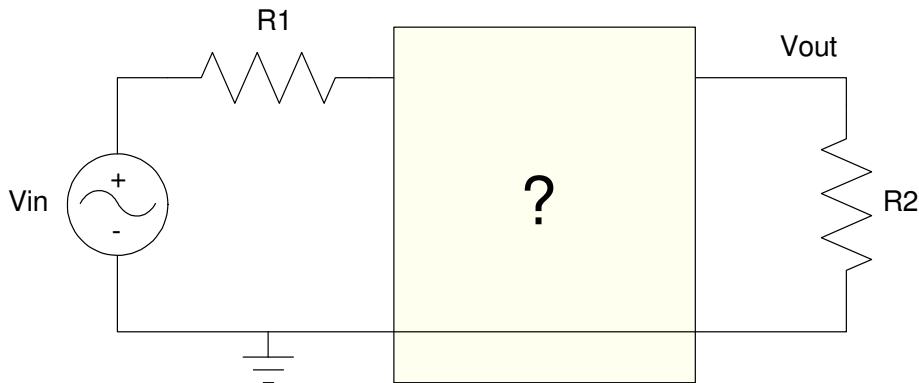
- $V_{in} = 1\text{mV}$  @ 1kHz
- $R_1 = 0 \text{ Ohms}$
- $R_2 = X \text{ Ohms}$

results in  $V_{out} = 37\text{mV}$

Assume

- $X = 1100 + 100*(\text{your birth month}) + (\text{your birth date}) \text{ Ohms}$
- $A_i = 0$

$X$ $1100 + 100*\text{mo} + \text{day}$	$R_{in}$	$A_i$	$R_{out}$	$A_o$
<b>1614</b>	<b>4957</b>	<b>0</b>	<b>872</b>	<b>57</b>



$A_o$  comes from case 1:

$$A_o \approx \left( \frac{57\text{mV}}{1\text{mV}} \right) 57\text{mV}$$

$R_{in}$  comes from case 2:

$$V_{out} = \left( \frac{R_{in}}{R_1 + R_{in}} \right) 57\text{mV} = 43\text{mV}$$

$$R_{in} = \left( \frac{43\text{mV}}{57\text{mV} - 43\text{mV}} \right) 1614 = 4957\Omega$$

$R_{out}$  comes from case 3

$$V_{out} = \left( \frac{R_2}{R_2 + R_{out}} \right) 57\text{mV} = 37\text{mV}$$

$$R_{out} = \left( \frac{57\text{mV} - 37\text{mV}}{37\text{mV}} \right) 1614 = 872\Omega$$

6) Assume X and Y are related by the following transfer function

$$Y = \left( \frac{100(s+m)}{(s^3+ms^2+ds+10)} \right) X$$

$$x(t) = 4 + 5 \cos(mt) + d \sin(mt)$$

where

- m is your birth month (1..12), and
- d is your birth date (1..31)

Find y(t)

m birth month (1..12)	d birth date (1..31)	y(t)
<b>5</b>	<b>14</b>	$y(t) = 200 - 52 \cos(5t) - 64 \sin(5t)$

$$Y = \left( \frac{100(s+5)}{(s^3+5s^2+14s+10)} \right) X$$

$$x(t) = 4 + 5 \cos(5t) + 14 \sin(5t)$$

DC:

$$s = 0$$

$$Y = \left( \frac{100(s+5)}{(s^3+5s^2+14s+10)} \right)_{s=0} \cdot (4) = 200$$

AC:

$$s = j5$$

$$Y = \left( \frac{100(s+5)}{(s^3+5s^2+14s+10)} \right)_{s=j5} \cdot (5 - j14) = -52.00 + j64.00$$

$$y(t) = -52 \cos(5t) - 64 \sin(5t)$$

Total answer

$$y(t) = 200 - 52 \cos(5t) - 64 \sin(5t)$$