ECE 111 - Homework #10

ECE 343 Signals & Systems- Due Due 8am, Tuesday, March 29th Please submit as a Word or pdf file and email to Jacob_Glower@yahoo.com with header ECE 111 HW#10

1) A filter has the following transfer function

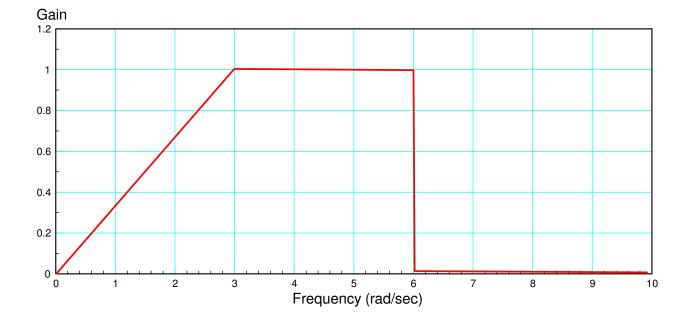
$$Y = \left(\frac{6s+30}{s^2+6s+60}\right)X$$

- 1a) What is the differential equation relating X and Y?
- 1b) Find y(t) assuming x(t) = 5
- 1c) Find y(t) assuming $x(t) = 5\cos(7t)$
- 2) Plot the gain vs. frequency for this filter from 0 to 50 rad/sec.

$$Y = \left(\frac{6s+30}{s^2+6s+60}\right)X$$

Problem 3-5) Design a filter of the following form so that the gain matches the graph below:

$$G(s) = \left(\frac{as}{\left(s^2 + bs + c\right)\left(s^2 + ds + e\right)\left(s^2 + fs + g\right)}\right)$$



- 3) Write an m-file, cost.m, which
 - Is passed an array, z, with each element representing (a, b, c, d, e, f, g)
 - Computes the gain, G(s) for this value of (a, b, c, d, e, f, g)
 - Computes the difference between the gain, G, and the target (above), and
 - Returns the sum-squared error in the gain

4) Use your m-file to determine how 'good' the following filter is:

$$G(s) = \left(\frac{as}{(s^2 + bs + c)(s^2 + ds + e)(s^2 + fs + g)}\right) = \left(\frac{85s}{(s^2 + 2s + 2)(s^2 + 2s + 5)(s^2 + 2s + 17)}\right)$$

5) Use fminsearch() to find the 'best' filter of the form

$$G(s) = \left(\frac{as}{\left(s^2 + bs + c\right)\left(s^2 + ds + e\right)\left(s^2 + fs + g\right)}\right)$$

- 5a) Give the resulting (a, b, c, d, e, f, g)
- 5b) Give the resulting filter, and
- 5c) Plot the 'optimal' filter's gain vs. frequency